

## How Good are the Fuel-Reduction Measures on Your Ship?

Objective: Estimate the *expected average change in fuel consumption* due to fuel-reduction measures of *any* kind for a given ship, whether by route planning (using NAVTRONIC) or by other ship optimization.

Given:

1. Power-speed ( $P$ - $V$ ) data collected for the ship under a range of steady-state sailing conditions, *before* and *after* implementing fuel-reduction measures.
2. A customary power-law fit to each data set,

$$P = a_1 V^{b_1} \text{ before,} \quad P = a_2 V^{b_2} \text{ after} \quad (1)$$

Apply the Performance Metric:

$$\overline{\Delta E_{rel}} = \left\{ \frac{a_2}{a_1} \overline{V^{(b_2-b_1)}} + (b_2 - 1) \overline{\Delta V_{rel}} - 1 \right\} \times 100 \% \quad (2)$$

$\overline{\Delta E_{rel}}$  Expected average relative change of total energy (hence fuel) consumption, expressed as a percent. Its value will be *negative* ( $\overline{\Delta E_{rel}} \leq 0$ ) when energy and fuel are *reduced*. The NAVTRONIC goal is  $\overline{\Delta E_{rel}} \leq -7\%$  through route planning for instance. The metric (2) holds for changes  $|\overline{\Delta E_{rel}}|$  smaller than 20 %. The dimensions of variables in (2) are those used in the power law (1).

$P$  Available propulsion power. Typically 60 % of the total power into the propeller shaft(s).

$V$  Forward speed of the ship through water.

$(a_1, b_1)$  Best-fit power-law coefficients for *before* (1) and *after* (2) sailing data (see equation (1) above).  
 $(a_2, b_2)$  Special methods are required when fitting a power law to actual sailing data. See the NAVTRONIC RTD Partner Technical Note, “*Fitting a Power Law to Ship Power-Speed Data*”, Apr 2013.

$\overline{V^{(b_2-b_1)}}$  Expected average ship speed  $V$  raised to the power of the difference in exponents ( $b_2 - b_1$ ) in future sailings. If past sailing data is believed to be representative of future sailing, and if  $f_i$  is the relative frequency of occurrence of speed  $V_i$  in a histogram of the steady-state speeds in past sailing data, then  $\overline{V^{(b_2-b_1)}} \approx \sum_i f_i V_i^{(b_2-b_1)}$ , with  $\sum_i f_i = 1$ . If future sailing speeds are expected to differ from past (because sailing constraints or modes of business have changed), then set  $f_i$  to the relative frequencies expected for future sailings. If the expected ship speeds are uniformly distributed between  $V_A$  and  $V_B$ , then  $\overline{V^{(b_2-b_1)}} = (V_B^c - V_A^c) / [c(V_B - V_A)]$  with  $c = b_2 - b_1 + 1$ .

$\overline{\Delta V_{rel}}$  Additional average relative change in speed (throttle), *not* included in  $V$  of  $\overline{V^{(b_2-b_1)}}$ , instituted at the discretion of the captain for *future* sailings, perhaps in response to evidence for or against successful fuel reduction measures, perhaps in connection elsewhere with counter-piracy measures.  $\overline{\Delta V_{rel}} = 0$  if no change in throttle is expected. If a 10 % average speed *reduction* is foreseen (or hypothesized), then  $\overline{\Delta V_{rel}} = -0.10$ .  $\overline{\Delta V_{rel}}$  is dimensionless.  $|\overline{\Delta V_{rel}}|$  is assumed to be small (less than 0.2).

Disclaimer: Equation (2) was developed and is under test in NAVTRONIC. It is floated here for discussion purposes. Derivation and examples with sailing data are in NAVTRONIC deliverables.

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